

Mathomatic User Guide

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Mathomatic User Guide

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Mathomatic Command Reference

Introduction

Mathomatic is an easy to use and colorful algebra calculator that can symbolically:

- combine and solve equations containing many variables,
- completely simplify and compare mathematical expressions and equations,
- do simple calculus transformations and series,
- perform quick real number, complex number, modular, and polynomial arithmetic,
- generate efficient C, Java, or Python language code from simplified equations,
- plot expressions with gnuplot in two or three dimensions, etc.

The name "Mathomatic" is a portmanteau of "math" and "automatic". It is a unique computer algebra system (CAS), in that all constants are one or more floating point values. All numeric arithmetic is IEEE standard floating point arithmetic, which most computers do very quickly. Mathomatic is written entirely in C, which is like a CAS written in assembly language, running as fast as the computer allows without any high-level language overhead.

Mathomatic is exceptionally good at solving, differentiating, simplifying, and calculating elementary algebra. It is designed with a simple command-line interface (CLI) that tries to be helpful. All input and output is line



at a time ASCII text. By default, input is standard input and output is standard output.

History

Mathomatic has been developed and supported almost every day by George Gesslein II, with help from the Internet community.

Mathomatic development started in the year 1986 to test new ideas and as an experiment in computerized mathematics, originally using the Microsoft C compiler for DOS and a text editor as the only development tools. Versions 1 and 2 were published by Dynacomp of Rochester, New York in 1987 and 1988 as a scientific software product for DOS. Afterwards it was released as shareware and then emailware, with a 2D equation graphing program that could find asymptotes, written in Microsoft C for DOS. At the turn of the century, Mathomatic was ported to the GNU C Compiler (gcc) under Linux and became free and open source software by publishing under the GNU Lesser General Public License. The graphing program was discontinued; 2D/3D graphing of equations is now accomplished with gnuplot.

Mathomatic is currently developed and maintained on a Ubuntu Linux x86-64-bit computer.

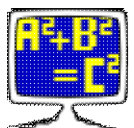
Developer Information

Building Mathomatic from source requires a C compiler with the standard C libraries. If compiled with the GCC C compiler for a Unix-like operating system, no changes need to be made to the source code. See the file *README.txt* for compilation instructions.

Mathomatic can easily be ported to any computer with at least 1 megabyte of free RAM. In the standard distribution, found on the Mathomatic home page, the maximum memory usage defaults to 400 megabytes (the version command tells this). Maximum memory usage is not reached unless all equation spaces are filled. The default maximum memory usage should be less than the amount of free RAM, and is adjusted by changing the `DEFAULT_N_TOKENS` define in the C include file *am.h* and recompiling. Memory usage can also be adjusted at startup with the **-m** option.

The Mathomatic source code can also be compiled as a symbolic math library that is callable from any C compatible program. See the file *lib/README.txt* for more developer information and how to include Mathomatic in your program.

Very little disk space (a few megabytes) is required to compile, install, and run the Mathomatic application. A readline library must be installed to compile-in and use readline (package called "libreadline-dev"), which allows editing and history recall of all Mathomatic line input by pressing the cursor keys.



Startup

SYNOPSIS

```
mathomatic [ options ] [ input_files or input ]
rmath [ input_files ]
```

To start the compiled, interactive Mathomatic application, run a terminal emulator which opens a shell window, and type "mathomatic" at the shell prompt (without double quotes). If m4 (macro) Mathomatic was installed, you may type "rmath" instead, to use Mathomatic with input of functions like $\sin(x)$ and \sqrt{x} allowed and automatically expanded to equivalent algebraic expressions. Logarithm function input is currently not available, because the logarithm function has not yet been implemented in the Mathomatic symbolic math engine.

If you are wondering what to try first in Mathomatic, type "help examples" at the Mathomatic prompt.

Color mode is toggled by the **-c** option on the shell command line, like this:

```
$ mathomatic -c
```

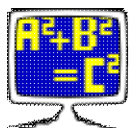
ANSI color mode is the default, which outputs ANSI terminal escape sequences to make each level of parentheses a different color, improving readability. If ANSI color mode is on, an ANSI compatible terminal emulator is required. If the colors are hard to see, use the **-b** option instead, which will always turn on bold color mode, increasing the color brightness.

The other options are described in the Unix/Linux man page for Mathomatic. After any options, text files may be specified on the shell command line that will be automatically read in with the read command, unless the **-e** option is specified, in which case mathematical expressions and Mathomatic commands are expected, separated by unquoted space characters.

It is recommended that the name *mathomatic* be shortened to *am* and *e* for quicker and easier access from the shell command line. This can be done in the Bash shell by adding the following two lines to your *~/.bashrc* file:

```
alias am=mathomatic
alias e="mathomatic -e --"
```

Then just typing "am" at the shell prompt will run Mathomatic as an interactive application. Typing "e" followed by a quoted mathematical expression at the shell prompt will quickly and silently bring up Mathomatic and calculate and display the result. "am" stands for "algebraic manipulator", and "e" stands for "evaluate".



Equations and Expressions

On the World Wide Web are some high quality pages with basic algebra definitions.

Mathematical equations and expressions are entered into Mathomatic **equation spaces** by typing, pasting, or reading them in at the main prompt. The maximum number and size of available equation spaces is displayed every time Mathomatic starts up. When an expression grows larger than half the equation space size, processing stops and the "Expression too large" message is displayed, returning you to the main prompt.

Each equation space is successively numbered with an **equation number** (starting at 1). The main prompt "1-> " contains the equation number of the current equation space. The current equation can be changed by typing a valid equation number at the main prompt (called selecting an equation space), or by entering another equation or expression, which becomes the current equation.

Any previously entered expression can be automatically entered again by entering a "#" followed by the relative or absolute equation space number of that expression. If this is entered first thing at the main prompt, it means something entirely different, that you are selecting that equation space; Otherwise, the RHS or expression at that equation space is substituted, for your convenience.

Equations

To enter an equation into the first available equation space and make it the current equation, simply type it in at the main prompt. Each equation space consists of two equation sides, called the Left-Hand Side (LHS) and the Right-Hand Side (RHS), separated by an equals sign (=). Each equation side consists of a mathematical expression, which is a mix of constants, variables, and operators, mostly in standard algebraic infix notation. Parentheses are used to override operator precedence and group things together. Valid parentheses characters are () and {}.

Note that the equals sign does not make an assignment to any variables, it only signifies equality (sameness) between the results of evaluating the LHS and RHS. Shown here is a valid equation with its parts labeled:

equation				
variables			constant	
a	=	b	-	(c + 2)
			operators	
LHS			RHS	

In the above equation, the variable **a** is called the **dependent** variable because its value depends on the **independent** variables **b** and **c**. In Mathomatic, any variable can be made the dependent variable by simply typing the variable name in at the prompt. This will solve the current equation for that variable and, if successful, make that variable the LHS.



Here is the above equation entered into Mathomatic and solved for **b**, then calculated for the values **a=1** and **c=1**:

```
1-> a=b-(c+2)

#1: a = b - c - 2

1-> b

#1: b = 2 + c + a

1-> calculate
Enter a: 1
Enter c: 1

b = 4

1->
```

The "#1:" listed in front of each displayed equation always indicates the equation space number it is stored in.

Mathomatic automatically does both symbolic and numeric mathematics computations during any manipulations. This means that it can handle algebraic formulas, as well as numbers. What follows is a simple example of the result of both types of computations working together during equation simplification and solving:

```
1-> 3*(x-1) + 1 = 2x + 1

#1: (3*(x - 1)) + 1 = (2*x) + 1

1-> simplify

#1: (3*x) - 2 = (2*x) + 1

1-> solve verify x

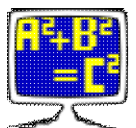
#1: x = 3

Solution verified.
1->
```

The "solve verify" command, used above, solves the current equation and then verifies the result by plugging the result into the original equation and simplifying. If an identity results (the LHS is identical to the RHS), a "Solution verified" message is displayed, otherwise "Solution might be incorrect" is displayed.

Expressions that are not equations

Non-equations, that is any mathematical expression without an equals sign, may be entered into equation spaces too. However, if the expression entered at the main prompt contains no variables, it will only be



calculated and displayed, unless the autocalc or auto option is turned off. Non-equations cannot be solved.

Constants

In Mathomatic, numeric arithmetic is double precision floating point with about 14 decimal digits accuracy. Many results will be exact, because symbolic math is an exact math, and because multiple floating point numbers can be combined for a single mathematical value; for example: $2^{(1/3)}$, which is the cube root of 2 exactly.

Constants are approximated real numbers stored internally as IEEE 754 standard 64-bit (8 bytes) double precision floating point values. They may be entered as decimal (base 10) numbers in normal notation or in scientific notation (also called exponential notation). Constants may also be entered in hexadecimal (base 16) by prepending them with "0x".

Constants are displayed in decimal (base 10, rounded to 14 digits) using either normal or scientific notation, whichever is shortest. Results are usually accurate from 12 to 14 digits, due to accumulated round-off error, because all constants are stored internally as double precision (rounded to 15 decimal digits) floats. And the amount of round-off error is not tracked, making Mathomatic unsuitable for applications requiring high precision, like astronomical calculations.

Excepting constants with a name (like "inf" for the infinity constant), constants always start with a decimal digit (0..9) or a period.

Examples of equivalent constants follow:

Normal Notation (base 10)	Scientific Notation (base 10)	Hexadecimal Notation (base 16)
10	1e1 (1.0 times 10^1)	0xa
.125	1.25e-1 (1.25 times 10^{-1})	0x.2
255	2.55e2 (2.55 times 10^2)	0xff

The exact syntax to enter constants as above may be found by looking up the C library function `strtod(3)`. In the Unix shell, "man strtod" will do that.

- The largest valid constant is **$\pm 1.797693e+308$** (slightly less than 2^{1024}).
- The smallest valid constant is **$\pm 2.225074e-308$** or 0.

The infinity constant is entered by typing "inf". Positive and negative infinity are distinct and understood, however division by zero produces one infinity value, not the two-valued \pm infinity which would be more correct. Also, floating point overflow produces either positive or negative infinity.

```
1-> 1/0
Warning: Division by zero.
```

```
answer = inf
```



```
1-> 0/0
Warning: Division by zero.
```

```
answer = nan
```

```
1->
```

nan or *NaN* stands for **Not a Number** and it means an invalid or indeterminate floating point arithmetic result. *NaN* cannot be directly entered into Mathomatic. The appearance of the constant *NaN* in an expression means the expression is unusable.

Fractions (such as **100/101**) are preserved if the numerator and denominator are not large. Fractions are always presented in fully reduced form; for example, **6/9** is converted to the irreducible fraction **2/3**. Constants which are exactly equal to a fraction are converted and displayed as fully reduced fractions; for example, **0.5** converts to **1/2**. Mathomatic internally converts a fraction to a single floating point value, then may convert it back to a fraction for display after all floating point arithmetic has been done, if the result is equal to a fraction.

Irrational numbers, such as the square root of two (**2^(1/2)**) and **pi**, are preserved and simplified for exactness, unless explicitly approximated.

Denominators of fractions are usually rationalized in Mathomatic; for example, **1/(2^(1/2))** becomes the equivalent **(2^(1/2))/2** upon simplification. This can be turned off with the command "set no rationalize_denominators".

Variables

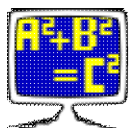
Variables are what Mathomatic is all about. That is where the term "symbolic" comes from, because variables are symbolic in nature. They are symbols that can represent known or unknown values, or any expression. Variables need not be defined in Mathomatic, just entering the variable name is enough.

Variable names consist of any combination of letters (a..z), digits (0..9), and underscores (_). They never start with a digit. By using the "set special_variable_characters" command, you can add to the allowed variable name characters. By default, letters in variable names are case sensitive, meaning the alphabetic case of each letter in the variable name is important. For example, variables named "A1" and "a1" represent two different variables, unless "set no case_sensitive" is entered beforehand.

The following variables are predefined and are not normal variables:

e, **ê**, or **e#** - the universal constant e (2.718281828...)
pi, **π**, or **pi#** - the universal constant π (3.1415926...)
i, **î**, or **i#** - the imaginary unit (square root of -1)
sign, **sign1**, **sign2**, ... - may only be +1 or -1
integer, **integer1**, ... - may be any integer value

The above can be used anywhere variables are required.



To automatically enter multiplication by a unique, two-valued "sign" variable, precede any expression with "+/-".

Operators

Mathomatic implements the standard rules of algebra for addition (+), subtraction (-), multiplication (*), division (/), modulus (%), and all forms of exponentiation (^ or **). An example of a rule of algebra is $2*x + 3*x$ being simplified to $5*x$.

All available operators are at least numerically capable (most are symbolically capable too, see above paragraph) and have precedence decreasing as indicated:

```
! factorial (same as gamma(x+1) function; highest precedence)
** or ^ power (exponentiation; high precedence)
* multiply      / divide      % modulus      // integral divide
+ add          - subtract or negate
= equate (lowest precedence)
```

Higher precedence operators are grouped (or evaluated) first, then multiple operators of the same precedence level are grouped left to right. This is called the "order of operations".

The default operator is multiply (*). If an expression (operand) is entered when an operator is expected, a multiply operator is automatically inserted. For example, entering $2x$, $2(x)$, and $(2)(x)$ all result in the expression $2*x$.

The modulus operator ($a \% b$) (spoken as "a modulo b") gives the remainder of the division (a / b), which allows modular arithmetic; also known as clock arithmetic, because the numbers wrap around, after they reach the modulus. Mathomatic can simplify, calculate, and even solve modular arithmetic! Using "integer" variables allows further modulus simplification when using the simplify command. An integer variable is specified by using a variable name that starts with "integer", like "integer1", "integer_x", etc. The resulting sign of any numerical modulus operation depends upon the "set modulus_mode" option.

The integral divide operator ($a // b$) divides a by b and then truncates by zeroing the fractional part to make the result an integer. For example, $(8 // 3)$ results in 2, which is useful when doing integer arithmetic. This operator currently implements no rules of algebra, and will not evaluate if an operand is a complex number.

Factorials $x!$ use the gamma function $\text{gamma}(x+1)$, so that the factorial operator works with any real number, not just the positive integers. The factorial operator currently implements no rules of algebra, and will not evaluate for complex numbers or if an overflow happens.

Absolute value notation is allowed, $|x|$ is converted to $(x^2)^{.5}$. This is not the same as standard absolute value where the real and imaginary parts of complex numbers are separated and then squared, but it works the same when given real number values with no imaginary units. The absolute value operation $|x|$ results in a positive value for any x value; that is, if -1 is a factor, it is removed.



Order of Operations example

The following example shows why operator precedence is important. Given the numerical expression:

$$64 / (-2)^4 + 6 * (3+1)$$

Mathomatic will parenthesize the highest precedence operators first: power, then times and divide. Addition and subtraction are the lowest precedence, so no need to parenthesize them. The result will be:

$$(64 / ((-2)^4)) + (6 * (3+1))$$

This is evaluated by combining constants from left to right on the same level of parentheses, deepest levels first. So the calculations are performed in the following order:

$(64/16) + (6*4)$	Combine deepest level parentheses first.
$4 + 24$	Divided 64 by 16 and multiplied 6 by 4.
28	Added 24 to 4.

If the calculations were performed in a different order, the result would be different.

Complex Numbers

Mathomatic automatically performs complex number addition, subtraction, multiplication, division, and exponentiation. It can also approximate roots of real and complex numbers, giving a single result; when multiple results are possible, the first real number result is chosen.

Complex numbers are of the form:

$$a + b*i$$

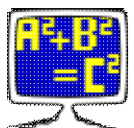
where **a** is the real part (a real number) and **b** is the imaginary part (an imaginary number). **i** is the "imaginary unit" and it represents the square root of -1 ("**-1**^.5" in Mathomatic notation).

The imaginary unit **i** may appear anywhere within an expression, as many times as you want, Mathomatic will handle and simplify it properly.

As an example of imaginary numbers being produced, **(-2)^.5** will be converted to **(2^.5)*i**.

Roots of complex numbers, such as **i^.5** and **.5^i**, will be approximated, and only a single root will be produced, even though there may be many roots (see the roots command). That single root is called the "principal value", which may be unexpected and will often be inexact.

Because **1/i** correctly simplifies to **-i**, after significant manipulation different numerical results might be produced with complex numbers and division. This is normal, so the sooner the result of a complex expression is calculated, the better.



Conjugation of all complex numbers in the current equation is accomplished by typing the following command:

```
replace i with -i
```

Commands

Mathomatic has about 43 simple English commands that may be typed at the main prompt. Please consult the Mathomatic Command Reference, for detailed information on all commands.

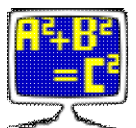
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Mathomatic Command Reference

Topics

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2. Entering Commands
3. Selecting Expressions
4. Solving Equations
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Commands

Approximate	Divide	Help	Pause	Replace	Taylor
Calculate	Echo	Imaginary	Plot	Roots	Unfactor
Clear	Edit	Integrate	Product	Save	Variables
Code	Eliminate	Laplace	Push	Set	Version
Compare	Extrema	Limit	Quit	Simplify	
Copy	Factor	List	Read	Solve	
Derivative	For	NIntegrate	Real	Sum	
Display	Fraction	Optimize	Repeat	Tally	

Mathomatic User Guide

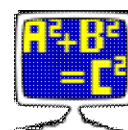
Introduction

LHS is shorthand for the Left-Hand Side of an equation. Similarly, **RHS** used here always means the Right-Hand Side.

In this document, text enclosed by straight brackets **[like this]** means it is optional and may be omitted. The word "expression" (without double quotes) always means a mathematical expression or formula.

At the Mathomatic main prompt, you may enter:

- A numerical expression, which is instantly evaluated and displayed with the calculate command; this is the autocalc option; with autocalc, the previously entered numerical expression is cleared.
- An algebraic expression or equation, which is stored and made the current equation.
- A variable to solve the current equation for (autosolve).
- An equation number to select as the current equation (autoselect).



- A slash (/) or pound sign (#) followed by a variable name to search all equations spaces forward or backward for.
- A Mathomatic command (listed in this document).
- A question mark (?) for quick, short help (same as the help command).
- A semicolon (;) followed by a comment; everything on a line after a semicolon is ignored.
- An exclamation point (!) followed by a shell or system command. "!" by itself invokes the default shell.

If a colon (:) starts the line, preceding any of the above input to the main prompt, it will always return with successful status, preventing any current read command operations from aborting.

Entering Commands

Mathomatic has about 43 commands that may be typed at the main prompt. Most commands operate on the current expression or equation by default. Commands are simple English words and are described below, in alphabetical order. If the command name is longer than 4 letters, you only need to type in the first 4 letters for Mathomatic to recognize the command. Option words and arguments for commands follow the command name and are separated by spaces. Commands are not executed until you press the Enter key, and any missing command line arguments that don't have a default are prompted for. For example, the Mathomatic command

```
help calculate
```

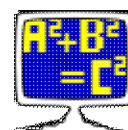
gives short help and usage information for the calculate command. "help" is the command, "calculate" is the argument (which is also a command, in this case).

Many commands have an optional **equation number range** argument, which specifies the equation spaces that the command is to operate on. An **equation number range** may be a single equation number, or a range of equation numbers separated by a dash (like "2-7", which means every equation space between and including equations 2 and 7), or the word "all", which specifies all equation spaces. If omitted, the current expression or equation is assumed. If pluralized as "**equation-number-ranges**" in the command syntax, that means multiple equation numbers and ranges may be specified for that command, separated by spaces.

A greater-than character (>) may be appended to the end of any command line, followed by a file name. This will redirect the output of the command to that file. If the file already exists, it will be overwritten without asking. Note that any debugging output will be redirected, too. Two greater-than characters (>>) next to each other will **append** command output to a file, like the Unix shell does. For example, the Mathomatic command

```
list export all >filename
```

will output all stored expressions and equations to a file in exportable, single-line per equation format, so they can be read in by a different math program. "list" is the command, "export" is the option word, and "all" is the **equation number range**.



Command option words, such as "export" in the above list command line, always come immediately after the command name and before anything else on the command line. These words direct the command to do a different, but related, task.

If Mathomatic becomes unresponsive (a rare occurrence), pressing Control-C once will usually safely abort the current operation and return you to the main prompt. If not, pressing Control-C three times in a row will exit Mathomatic, with a warning displayed the second time.

Selecting Expressions

Syntax: `#["+" or "-"]equation-number [new-expression]`

To change the current equation at the main prompt and display it or replace it, type a pound sign (#) followed by the equation space number you wish to select, possibly followed by a new expression to replace it with. The **equation number** may be preceded by plus (+) or minus (-), to select an equation relative to the current equation, instead of an absolute equation number. This syntax also works when prompted for an expression, the RHS or the expression at that equation number is substituted every place **#equation-number** is entered.

Autoselect feature: Selecting an equation space to make it the current equation is now conveniently done by typing only the **equation number** at the main prompt. This is called the "set autoselect" option.

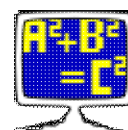
Solving Equations

Syntax: **variable** or "0"

Mathomatic can solve symbolic equations for any **variable** or for **zero**. Solving is accomplished internally by applying identical mathematical operations to both sides of the equation and simplifying, or by plugging the general coefficients of the solve variable into the quadratic formula. The Mathomatic solve algorithm is the best possible for general algebra, however the result is not verified by plugging the solutions into the original equation unless the "solve verify" command is used for solving.

To automatically solve the current equation for a variable, type the **variable** name at the main prompt. Mathomatic will proceed to manipulate the current equation until all of the solutions for the specified **variable** are determined. If successful, the current equation is replaced with the solutions and then displayed.

Automatic cubic (third degree), quintic (fifth degree), and higher degree polynomial equation solving is not supported. Some cubic and quartic polynomial equations can be manually solved with the general equations in files "tests/cubic.in" and "tests/quartic.in". Quartic (fourth degree) polynomial equations can be automatically solved if they are biquadratic; that is, containing only degree four, degree two, and degree zero terms of the solve variable. Biquadratic polynomial equations of any degree can be generally solved by Mathomatic



because they can be plugged into the quadratic formula.

Note that running the simplify command is a good idea after solving. The solve routine only unfactors the equation as needed to solve it and the result is not completely simplified.

To solve for zero, type in "0" at the main prompt. Zero solving is a special solve that will always be successful and will transform most divide operators into mathematically equivalent multiplications and subtractions, so that the result will more likely be a valid polynomial equation:

```
1-> a=b+1/b ; this is actually a quadratic equation
```

```
#1: a = b +  $\frac{1}{b}$ 
```

```
1-> 0 ; solve for zero
```

```
#1: 0 = (b*(b - a)) + 1
```

```
1-> unfactor ; expand, showing that this is a quadratic polynomial equation in "b"
```

```
#1: 0 = (b^2) - (b*a) + 1
```

```
1-> b ; solve for "b"
Equation was quadratic.
```

```
#1: b =  $\frac{(((a^2) - 4)^{\frac{1}{2}} * \text{sign1}) + a}{2}$ 
```

```
1-> a ; solve for "a", to check the answer
Raising both sides to the power of 2 and unfactoring...
```

```
#1: a =  $\frac{(b^2) + 1}{b}$ 
```

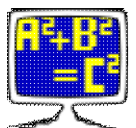
```
1-> simplify
```

```
#1: a = b +  $\frac{1}{b}$ 
```

```
1->
```

You can prefix the solve **variable** name with "=" to solve and swap equation sides, putting the solve variable on the right-hand side. Typing "=" by itself will only swap sides of the current equation and display.

To see all of the steps performed during a solve operation, type "set debug 2" before solving.



Approximate command

Syntax: **approximate** [equation-number-ranges]

This command operates on the current or specified equation spaces. It substitutes the special universal constants **pi** and **e** with their respective floating point values and approximates all constants, roots, and surds. This allows them to combine with other constants and may help with simplification and comparisons.

Calculate command

Syntax: **calculate** ["factor"] [equation-number-range] [feedback-variable number-of-iterations]

This command is the formula calculator that prompts for the value of each normal variable in the RHS of the current or specified equations or expressions. It then temporarily substitutes any entered values, and simplifies, approximates, and substitutes all "sign" variables with all possible combinations of values (+1 and -1), displaying each solution as it does so. If all variables are supplied with constant values, then each solution will be a constant, otherwise the result will contain the variables you didn't enter values for. Nothing is modified by this command.

This command is used to temporarily plug in values and approximate expressions and expand "sign" variables. When an expression with only numbers is entered at the main prompt, this calculate command is automatically invoked on it, displaying the calculated result without storing.

If there are any simple numerical fractions in the result, those are displayed alongside any short result.

To only simplify and expand "sign" variables in stored expressions without approximating, use the "simplify sign" command instead.

If a **feedback variable** and **number of iterations** are specified on the calculate command line, you will be prompted for the initial value of the **feedback variable**, and the calculation will be iterated, with the simplified result repeatedly plugged back into the **feedback variable**. This will be done until convergence (the output equals the input) or when the specified **number of iterations** have been performed (if non-zero), whichever comes first. To see all of the intermediate values, type "set debug 1" before this.

"calculate **factor**" factorizes all integers and variables before display.

Examples of using the calculate command:

```
1-> y=x^2+x
```

```
#1: y = (x^2) + x
```




```
1-> x ; solve for x
Equation is a degree 2 polynomial in x.
Equation was quadratic.
```

$$\#1: x = \frac{-1 \cdot (1 + (((1 + (4 \cdot y))^{\frac{1}{2}}) \cdot \text{sign}))}{2}$$

```
1-> calculate
Enter y: 0
There are 2 solutions.
```

```
Solution number 1 with sign = 1:
x = -1
```

```
Solution number 2 with sign = -1:
x = 0
```

```
1->
```

An example of iteration:

```
1-> x_new=(x_old+(y/x_old))/2 ; iterative formula for calculating the square root of y
```

$$\#2: x_{\text{new}} = \frac{(x_{\text{old}} + \frac{y}{x_{\text{old}}})}{2}$$

```
2-> calculate x_old 1000 ; iterate up to 1000 times to calculate the square root of 100
Enter y: 100
Enter initial x_old: 1
Convergence reached after 9 iterations.
```

```
x_new = 10
```

```
2->
```

Clear command

Syntax: **clear** [equation-number-ranges]

This command clears the specified equation spaces so that they are empty and can be reused. They are deleted from RAM only.



"clear all" quickly clears all equation spaces and restarts Mathomatic, resetting internal memory and deleting all expressions stored in RAM, without losing your settings.

Code command

Syntax: `code ["c" or "java" or "python" or "integer"] [equation-number-ranges]`

This command outputs the current or specified equations as floating point or integer assignment statements in C, Java, or Python programming language code. The default is C double precision floating point code. The output from this command should compile correctly and emulate the equation from Mathomatic, if no warnings are given.

With "code integer", integer arithmetic is assumed, otherwise double precision floating point arithmetic is assumed. "code integer" is more generic and should work with any language.

To represent factorials, the user supplied function `fact()` is called, since there is no equivalent function or operator in these languages. `fact()` functions for several languages are supplied in the directory *examples* in the Mathomatic source distribution.

For the most efficient code, use the `simplify` and `optimize` commands on your equations before running this code command.

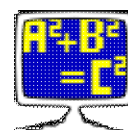
The C and Java languages require that all variables be defined before use. The `variables` command is provided for this. The output of the `variables` command should be prepended to the output of the code command before compiling.

Compare command

Syntax: `compare ["symbolic"] ["approximate"] equation-number ["with" equation-number]`

This command compares two equation spaces to see if they are mathematically the same (equal). If only one **equation number** is supplied, the comparison is between the current equation and the specified equation. The comparison will be faster and more accurate if both equations are previously solved for the same variable.

The `simplify` command is automatically used on both expressions if needed. If this compare command says the equations or expressions are identical, then they are definitely identical. If this command says the equations or expressions differ, then they might be identical if they are too hard for Mathomatic to simplify completely.



The "symbolic" option uses the "simplify symbolic" option when simplifying. This option sometimes simplifies more, but is not 100% mathematically correct.

The "approximate" option runs the approximate command on both expressions or equations. This makes the compare command more likely to succeed.

"repeat compare" simplifies fully instead of just once, making the compare more likely to succeed too.

Another way of comparing expressions by simply setting them equal is a convenient way of checking validity too, with Mathomatic. You just solve for any variable to see if it is an identity, or solve for zero. If it is an identity, both equations sides are mathematically equivalent and identical.

Copy command

Syntax: **copy** [equation-number-ranges]

This command simply duplicates the current or specified equation spaces. The new, duplicated expressions are stored in the next available equation spaces and displayed, along with their new equation numbers.

Derivative command

Syntax: **derivative** ["nosimplify"] **variable** or "all" [order]

Alternate command name: **differentiate**

This command computes the exact symbolic derivative of a function with respect to the specified **variable**, using the current expression or RHS of the current equation as the function. It does this by recursively applying the proper rule of differentiation for each operator encountered. The result is fully simplified with the simplify command, unless the "nosimplify" option is specified. If successful, the derivative is placed in the next available equation space, displayed, and becomes the current equation. The original equation is not modified.

Specifying "all" computes the derivative of the current expression with respect to all normal variables. It is equivalent to adding together the derivatives with respect to each variable.

Specifying the **order** allows you to repeatedly differentiate and simplify. The default is to differentiate once (**order**=1).

If differentiation fails, it is probably because symbolic logarithms are required. Symbolic logarithms are not implemented in Mathomatic, yet. Also, the factorial, modulus, and integral divide operators cannot be differentiated if they contain the specified **variable**. Because this command handles almost everything, a



numerical differentiation command is not needed.

Some examples:

```
1-> x^3+x^2+x+1
```

```
#1: (x^3) + (x^2) + x + 1
```

```
1-> derivative ; no need to specify the variable if there is only one
Differentiating with respect to (x) and simplifying...
```

```
#2: (3*(x^2)) + (2*x) + 1
```

```
2-> a*x^n
```

```
#3: a*(x^n) ; show a general rule of differentiation
```

```
3-> derivative x
Differentiating with respect to (x) and simplifying...
```

```
#4: a*n*(x^(n - 1))
```

```
4-> integrate x ; undo the differentiation
```

```
#5: a*(x^n)
```

```
5->
```

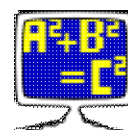
Display command

Syntax: **display** ["factor"] ["mixed"] [equation-number-ranges]

This command displays stored expressions in nice looking multi-line 2D (two-dimensional) fraction format, where division is displayed as a numerator over a fractional line (made up of dashes) over a denominator. If the width (number of columns) required for this 2D display exceeds the screen width, the expression is displayed instead in single-line (one-dimensional) format by the list command. The screen width is set automatically on startup, or by the "set columns" option.

Non-integer constants are converted to reduced fractions, if they are exactly equal to a simple fraction and it would improve readability.

The "factor" option causes all integers, less than or equal to 15 decimal digits long, to be factorized into their prime factors before display, including the numerator and denominator of fractions. To always factorize integers like this before display, use the "set factor_integers" option.



The "mixed" option displays mixed fractions when possible. A mixed fraction is an expression like $(2+(1/4))$, rather than the simple fraction $9/4$. To always display mixed fractions, use the "set fractions mixed" option.

Divide command

Syntax: **divide** [**base-variable**] [**dividend divisor**]

This command is for doing and experimenting with polynomial and numerical division and Greatest Common Divisors (GCD). It simply prompts for two expressions and divides them, displaying the result and the GCD. Mathomatic has general symbolic polynomial division and GCD routines used by the simplify command which this divide command calls without any other processing if two polynomials are entered.

This command prompts for the **dividend** (the main polynomial) and then the **divisor** (what you want to divide the main polynomial by). The polynomial quotient, remainder, and GCD are displayed. The power of the highest power term in the dividend must be greater than or equal to the power of the highest power term in the divisor, otherwise the polynomial division will fail (as it should). In other words, the degree of the divisor polynomial must be less than or equal to the degree of the dividend polynomial.

A **base variable** may be specified first on the command line as the base variable of the two polynomials, but is usually not necessary because a good base variable is automatically selected.

If two numbers are entered instead of polynomials, the result of the numerical division, the GCD, and the Least Common Multiple (LCM) are displayed. The LCM of two numbers is the smallest positive number that can be evenly divided by both numbers separately, without remainder. The LCM is the same as the Lowest Common Denominator (LCD) of two fractions and is the two numbers multiplied together, divided by the GCD.

The Greatest Common Divisor of **a** and **b** is defined as the greatest positive number or polynomial that evenly divides both **a** and **b** without remainder. In Mathomatic, the GCD is not necessarily integer, unless both **a** and **b** are integers. The Euclidean GCD algorithm is used by Mathomatic to compute the GCD for numbers and polynomials.

The GCD is the best way to reduce any fraction to its simplest form. Just divide the numerator and denominator by their GCD, and replace each of them with their quotients (there will be no remainder); the result is a completely reduced, equivalent fraction. The GCD is also used when factoring polynomials and for simplifying.

The Euclidean GCD algorithm of successive divides is the best way to compute the GCD for numbers and polynomials. Multivariate polynomial GCD computation usually requires recursion of the GCD algorithm or other methods. Currently the polynomial GCD routine in Mathomatic is not recursive, making it univariate and simpler. Because it is univariate, Mathomatic might be unable to find the GCD of polynomials with many variables. Finding the GCD of large polynomials will probably not succeed anyways with floating point arithmetic, because of accumulated round-off error.



The polynomial division algorithm in Mathomatic is generalized and able to handle any number of variables (multivariate), and division is always done with one selected base variable to be proper polynomial division. Being generalized, the coefficients of the polynomials may be any mathematical expression not containing the base variable.

An example of polynomial division:

```
1-> divide
Enter dividend: (x^4) - (7*(x^3)) + (18*(x^2)) - (22*x) + 12
Enter divisor: (x^2) - (2*x) + 2

Polynomial division successful using variable (x).
The quotient is:
6 + (x^2) - (5*x)

The remainder is:
0

Polynomial Greatest Common Divisor (iterations = 1):
(x^2) - (2*x) + 2
1->
```

The number of iterations displayed is the number of polynomial divides done to compute the GCD with the Euclidean algorithm.

Echo command

Syntax: **echo** [text]

By default, this command outputs a line of **text**, followed by a newline.

```
repeat echo -
```

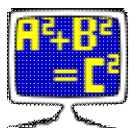
outputs a line of dashes.

```
repeat echo
```

clears the screen.

Edit command

Syntax: **edit** [file-name]



This command invokes the ASCII text editor specified by the EDITOR environment variable. By default, all equation spaces are edited. Access to shell (*/bin/sh*) is required for this command to work.

Type "edit" at the Mathomatic prompt to edit all expressions and equations you have entered for the current session. When you are done editing Mathomatic expressions and commands, save and exit the editor to have them automatically read in by Mathomatic. If Mathomatic gets an error reading in its new input, observe where the error is and continue, to automatically re-enter the editor.

To edit an existing file and have it read in, specify the **file name** on the edit command line.

Eliminate command

Syntax: **eliminate variables or "all" ["using" equation-number]**

This command is used to combine simultaneous equations, by automatically substituting variables in the current equation. It will scan the command line from left to right, replacing all occurrences of the specified **variables** in the current equation with the RHS of solved equations. The equation to solve can be specified with the "using" argument. If "using" is not specified, Mathomatic will search backwards, starting at the current equation minus one, for the first equation that contains the specified variable. The equation to solve is solved for the specified variable, then the RHS is inserted at every occurrence of the specified variable in the current equation. That effectively eliminates the specified variable from the current equation, resulting in one less unknown.

There is an advantage to eliminating multiple variables in one command: each equation will be used only once. If the same equation is solved and substituted into the current equation more than once, it will cancel out.

"eliminate all" is shorthand for specifying all normal variables on the command line. "repeat eliminate all" will eliminate all variables repeatedly until nothing more can be substituted, using each equation only once.

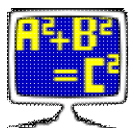
Here is a simple example of combining two equations:

```
1-> ; This arrives at the distance between two points in 3D space from the
1-> ; Pythagorean theorem (distance between two points on a 2D plane).
1-> ; The coordinate of point 1, 2D: (x1, y1), 3D: (x1, y1, z1).
1-> ; The coordinate of point 2, 2D: (x2, y2), 3D: (x2, y2, z2).
1->
1-> L^2=(x1-x2)^2+(y1-y2)^2 ; Distance formula for a 2D Cartesian plane.

#1: L^2 = ((x1 - x2)^2) + ((y1 - y2)^2)

1-> distance^2=L^2+(z1-z2)^2 ; Add another leg.

#2: distance^2 = (L^2) + ((z1 - z2)^2)
```



```

2-> eliminate L ; Combine the two equations.
Solving equation #1 for (L) and substituting into the current equation...

#2: distance^2 = ((x1 - x2)^2) + ((y1 - y2)^2) + ((z1 - z2)^2)

2-> distance ; Solve to get the distance formula for 3D space.

#2: distance = (((((x1 - x2)^2) + ((y1 - y2)^2) + ((z1 - z2)^2))^(1/2)) * sign2

Finished reading file "pyth3d.in".
2->

```

Extrema command

Syntax: **extrema** [**variable**] [**order**]

This command computes possible extrema (the minimums and maximums) of the current expression by default, or possible inflection points when **order** is 2. The result is placed in the next available equation space, displayed, and becomes the current equation. The original expression is not modified.

By default (**order**=1) this command computes stationary points. The stationary points of function **f(x)** are the values of **x** when the slope (derivative) equals zero. Stationary points are likely the local minimums and maximums of the function, unless the point is determined to be an inflection point.

For **y=f(x)**, where **f(x)** is the RHS and **x** is the specified **variable**, this command gives the values of **x** that make the minimums and maximums of **y**. This is computed by taking the derivative of **f(x)**, setting it equal to zero, and then solving for **x**.

The number of derivatives to take before solving can be specified by the **order** argument (default is 1). When **order** is 2, possible points of inflection are determined. A point of inflection is a point on a curve at which the second derivative changes sign from positive to negative or negative to positive.

```

1-> y=x^2

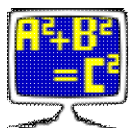
#1: y = x^2

1-> extrema x

#2: x = 0

2->

```



This function is a parabola, with the minimum at $x=0$.

Factor command

Syntax: **factor** ["number" [integers]] or ["power"] [equation-number-range] [variables]

Alternate command name: **collect**

This command will factorize manually entered **integers**, displaying all prime factors, when "**numbers**" is specified on the command line. Otherwise this command will factor **variables** in expressions in the specified equation spaces.

This command does not factor polynomials. To factor polynomials with repeated or symbolic factors, use the **simplify** or **fraction** commands. To factorize integers in equation spaces and display, use the "display factor" command.

"factor **number**" will prompt for an integer to factorize, which may be up to 15 decimal digits. The plural "factor **numbers**" will repeatedly prompt for **integers** to factorize, until an empty line is given. Multiple **integers**, integer ranges (two integers separated with a dash "-"), or multiple expressions that evaluate to integers, can be specified on the same line and should be separated with spaces.

Without the "number" option, this command will factor out repeated sub-expressions in equation spaces. When factoring expressions, this command does some basic simplification and factors out any common (equal) sub-expressions it can, unless **variables** are specified on the command line, in which case only common sub-expressions containing those variables are factored out. This collects together terms involving those variables.

For example, with the following expression:

$$(b*c) + (b*d)$$

variable **b** factors out and the result of this command is:

$$b*(c + d)$$

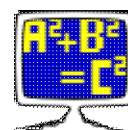
If no variables are specified on the command line, this command factors even more: the bases of common (equal) bases raised to any power are factored out. This is called Horner factoring or Horner's rule.

For example:

$$1 \rightarrow (2+3x)^2 * (x+y)$$

$$\#1: ((2 + (3 \cdot x))^2) \cdot (x + y)$$

$$1 \rightarrow \text{unfactor ; expand}$$



```
#1: (4·x) + (12·(x^2)) + (9·(x^3)) + (4·y) + (12·x·y) + (9·(x^2)·y)

1-> factor x ; collect terms containing x

#1: (x·(4 + (12·y))) + ((x^2)·(12 + (9·y))) + (9·(x^3)) + (4·y)

1-> x^3+2x^2+3x+4 ; enter another expression

#2: (x^3) + (2·(x^2)) + (3·x) + 4

2-> factor ; Horner factoring

#2: (x·((x·(x + 2)) + 3)) + 4

2->
```

"factor **power**" does only power operator collecting; that is, $(a^n) \cdot (a^m) \cdot (b^n) \cdot (b^m)$ is transformed to $(a \cdot b)^{(n+m)}$. With this option, **variables** cannot be specified.

To undo any kind of factoring in selected equation spaces, use the unfactor command.

For command

Syntax: **for** **variable** **start** **end** [**step-size**]

This command is good for testing an expression with many sequential input values. It quickly evaluates and displays the current expression for each value of the index **variable** as the index **variable** goes from **start** to **end** in steps of **step-size** (default 1). Nothing is modified.

The syntax of this command is the same as the sum and product commands. This command is not a programming construct, and only allows automatically plugging in sequential values of a **variable** in the current expression, displaying the results.

Fraction command

Syntax: **fraction** ["**numerator**"] ["**denominator**"] [**equation-number-range**]

This command reduces and converts expressions with any algebraic fractions in them into a single simple algebraic fraction (usually the ratio of two polynomials), similar to what Maxima's `rat()` function does. It does this by combining all terms added together with like and unlike denominators to a single simple fraction with a like denominator. Unlike denominators are combined by converting the terms to what they would be over like (common) denominators. Fractions are reduced by cancelling out the Greatest Common Divisor (GCD) of



the numerator and denominator.

The result of this command is mathematically equivalent to the original expression, unless the "numerator" or "denominator" option is specified, in which case the result is the numerator or denominator of the original expression. If both the "numerator" and "denominator" options are specified at once, this command will return with failure if the result is not a fraction, otherwise the entire fraction is returned.

Note that algebraic fractions added together with like denominators are automatically combined by almost any Mathomatic command. Polynomial factoring is only done by the simplify command and this fraction command, to improve simplification.

Example:

```
1-> 1/x+1/y+1/z
```

```
#1: 1 1 1
    - + - + -
    x y z
```

```
1-> fraction
```

```
#1: ((y + x) * z) + (x * y)
    (x * y * z)
```

```
1-> unfactor
```

```
#1: ((y * z) + (x * z) + (x * y))
    (x * y * z)
```

```
1-> unfactor fraction
```

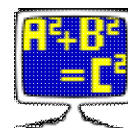
```
#1: 1 1 1
    - + - + -
    x y z
```

```
1->
```

"repeat fraction" repeatedly runs the fraction command until the result stabilizes to the smallest size expression or fraction.

If more simplification is needed, use the "simplify fraction" command instead.

Help command



Syntax: **help** [topics or command-names]

Alternate command name: ?

This command is provided as a quick reference while running Mathomatic. If the argument is a command name, a one line description and one line syntax of that command are displayed. Command names may be abbreviated.

Entering this command by itself will display a list of topics and commands. "help copyright" will display the copyright and license notice for the currently running version of Mathomatic.

To create a quick reference of all Mathomatic commands, type:

```
help all >quickref.txt
```

Imaginary command

Syntax: **imaginary** [variable]

This command copies the imaginary part of a complex number expression to the next available equation space. If the current expression or RHS of the current equation is not complex, the warning message "Expression is not a mix" will be displayed. A complex number expression contains both imaginary and real number parts. To copy only the real number part, see the real command.

The separation **variable** may be specified on the command line, the default is the imaginary unit **i**. **i** is really a mathematical constant equal to the square root of -1, but it can often be specified where variables are required in Mathomatic.

If successful, the result may contain the imaginary unit **i** or the specified separation **variable**.

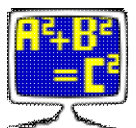
```
1-> (a+b*i)/(c+d*i)

      (a + (b*i))
#1:  -----
      (c + (d*i))

1-> imaginary

      i*((b*c) - (a*d))
#2:  -----
      (c^2 + d^2)

2->
```



Integrate command

Syntax: **integrate** ["constant" or "definite"] variable [order]

Alternate command name: **integral**

This command computes the exact symbolic integral of a polynomial function with respect to the specified **variable**, using the current expression or RHS of the current equation as the function. If successful, the simplified integral is placed in the next available equation space, displayed, and becomes the current equation.

The default is to compute and display the **indefinite integral**, also known as the **antiderivative** or **primitive**. The antiderivative is the inverse transformation of the derivative.

"integrate constant" simply adds a uniquely named **constant of integration** ("C_1", "C_2", etc.) to each integration result. The constants of integration here are actually variables that may be set to any constant.

"integrate definite" also integrates, but prompts you for the lower and upper bounds for **definite integration**. If **g(x)** is the indefinite integral (antiderivative) of **f(x)**, the definite integral is:

$$g(\text{upper_bound}) - g(\text{lower_bound})$$

Specifying the **order** allows you to repeatedly integrate. The default is to integrate once (**order**=1).

This command is only capable of integrating polynomials.

```
1-> x^3+x^2+x+1
```

```
#1: (x^3) + (x^2) + x + 1
```

```
1-> integrate x
```

```
#2: (x^4)  (x^3)  (x^2)
     ---- + ---- + ---- + x
      4      3      2
```

```
2-> derivative x ; check the result
```

```
Differentiating with respect to (x) and simplifying...
```

```
#3: (x^3) + (x^2) + x + 1
```

```
3-> compare 1
```

```
Comparing #1 with #3...
```

```
Expressions are identical.
```

```
3->
```



Laplace command

Syntax: **laplace** ["inverse"] **variable**

This command computes the Laplace transform of a polynomial function of the specified **variable**, using the current expression or RHS of the current equation as the function. If successful, the transformed function is placed in the next available equation space, displayed, and becomes the current equation.

This command only works with polynomials.

A Laplace transform can be undone by applying the **inverse** Laplace transform. That is accomplished by specifying the "inverse" option to this command.

```
1-> y=1
#1: y = 1

1-> laplace x ; compute the Laplace transform of 1
#2: y = 
$$-\frac{1}{x}$$


2-> a*x^n ; a general polynomial term
#3: a*(x^n)

3-> laplace x
#4: 
$$\frac{a*(n!)}{(x^{(n+1)})}$$


4-> laplace inverse x
#5: a*(x^n)

5->
```



Limit command

Syntax: **limit** *variable* *expression*

This command takes the limit of the current expression as **variable** goes to the specified **expression**. The result is always an equation and placed in the next available equation space and displayed.

L'Hopital's rule for taking limits is not used by this command. Instead the limit is taken by simplifying, solving, and substituting. This command is experimental and does not know about negative infinity and occasionally gives a wrong answer when dealing with infinities.

```
1-> 2x/(x+1)
```

```
#1: 
$$\frac{2 \cdot x}{(x + 1)}$$

```

```
1-> limit x inf ; take the limit as x goes to infinity
Solving...
```

```
#2: limit = 2
```

```
1->
```

List command

Syntax: **list** ["**export**" or "**maxima**" or "**gnuplot**" or "**hex**"] [*equation-number-ranges*]

This command displays stored expressions in single-line (one-dimensional) format. A single formatting option may be specified. With no option specified, expressions are displayed in decimal, Mathomatic format; The text result can then be entered or read back into Mathomatic.

Formatting options:

"list **export**" outputs expressions in a generally exportable, single-line text format. You can cut-and-paste the expressions or redirect them to a file, so they can be read in with a different math program.

"list **maxima**" is for making expression output compatible with the free computer algebra system Maxima.



"list **gnuplot**" is for making expression output that is compatible with the free graphing utility gnuplot.

"list **hex**" displays as normal (without these options), except constants are displayed as hexadecimal values in exponential notation, where no more precision is lost by display rounding. Display rounding happens only to the displayed value (not the stored value) and only if a floating point value is converted to decimal for display. Expressions that are displayed by this option can be read back into Mathomatic exactly as they were.

This list command simply outputs expressions and equations as stored internally by Mathomatic, translating them to the requested output format. There is no simplification and nothing more is done.

To display equation spaces in better looking multi-line fraction format, use the display command.

NIntegrate command

Syntax: **nintegrate** ["trapezoid"] **variable** [partitions [lower-bound upper-bound]]

This is a numerical integrate command that will work with almost any expression and will not generally compute the exact symbolic integral except for the simplest of expressions. This command will prompt you for the lower and upper bounds to perform numerical definite integration on the current expression or the RHS of the current equation, with respect to the specified **variable**. These bounds may be any expression not containing infinity.

This command uses Simpson's rule to do the approximation. Accuracy varies widely, depending on the expression integrated, the interval between the lower and upper bounds, and the number of **partitions**. The default is to split the interval into 1000 partitions. Setting the number of partitions greater than 10000 seldom is helpful, because of accumulated floating point round-off error.

If "trapezoid" is specified on the command line, the trapezoid method is used instead, which is usually less accurate than Simpson's rule. The way the trapezoid method works is: the interval from the lower bound to the upper bound is divided into 1000 **partitions** to produce 1000 trapezoids, then the area of each trapezoid is added together to produce the result. This means that the accuracy usually decreases as the interval increases. Simpson's rule uses the same method, with quadratic curves bounding the top of each trapezoid, instead of straight lines, so that curves are approximated better.

If the integration fails, chances of success are greater if you reduce the number of variables involved in the integration.

If there are any singularities, such as division by zero, between the bounds of integration, the computed result will be wrong.

Here is an example of successful numerical integration:




```
1-> y=x^0.5/(1-x^3)
```

```

      1
    (x^-)
      2
#1: y = -----
      (1 - x^3)

```

```
1-> nintegrate x
```

Warning: Singularity detected, result of numerical integration might be wrong.

Enter lower bound: 2

Enter upper bound: 4

Approximating the definite integral of the RHS
using Simpson's rule (1000 partitions)...

Numerical integration successful:

```
#2: y = -0.16256117185712
```

```
1->
```

This example avoids the singularity at $x=1$ and is accurate to 12 digits.

Optimize command

Syntax: **optimize** [equation-number-range]

This command splits the specified equations into smaller, more efficient equations with no repeated expressions. Each repeated sub-expression becomes a new equation solved for a temporary variable (named "temp").

Note that the resulting assignment statements may be in the wrong order for inclusion in a computer program with the code command; the order and generated code should be visually checked before using. The source code statements may need to be manually put in the right order to work properly.

```
1-> y = (a+b+c+d)^(a+b+c+d)
```

```
#1: y = (a + b + c + d)^(a + b + c + d)
```

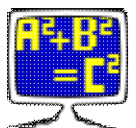
```
1-> optimize
```

```
#2: temp = a + b + c + d
```

```
#1: y = temp^temp
```

```
1-> eliminate temp ; undo the optimization
Solving equation #2 for (temp)...
```

```
#1: y = (a + b + c + d)^(a + b + c + d)
```



1->

Pause command

Syntax: **pause** [text]

This command waits for the user to press the Enter key. It is useful in text files (scripts) that are read in to Mathomatic. Optionally, a one line text message may be displayed.

Typing "quit" or "exit" before pressing the Enter key will fail this command and abort the current script.

This command is ignored during test mode and when input is not a terminal.

Plot command

Syntax: **plot** [equation-number-ranges] [xyz-ranges] [expressions,]

This command automatically plots the given mathematical **expressions** in 2D or 3D with the free graphing utility gnuplot. The specified equations are plotted at once, along with any comma separated expressions on the command line. Each expression should contain the variable **x** to be successfully plotted. If it also contains the variable **y**, a 3D surface plot is performed in Cartesian space, with the **x**, **y**, and **z** axes projected on your 2D display.

A gnuplot X range, Y range, and even a Z range may be specified on the plot command line. For example, "plot [-128:128]" will make the X axis go from -128 to 128, and "plot [-128:128] [-1:1]" will also make the Y axis go from -1 to 1. A pair of straight brackets [] must surround each range.

Plotting of an equation space with the imaginary number **i** in it is allowed, however plots are always plotted on real Cartesian space, showing only real number points. If there are no real number points, the plot will fail.

Gnuplot must be installed and accessible from shell by typing "gnuplot" for this command to work. All functions and operators of gnuplot can be used in the plot **expression**. If gnuplot fails, the gnuplot command line is displayed to show what failed. To always show the gnuplot command line, enter "set debug 1" beforehand, to set debug level 1 for the current session.

Plots may be customized. Typing "set **plot_prefix**" at the Mathomatic main prompt, followed by a string of 8-bit characters, will prepend the string to the gnuplot plot string, when using the Mathomatic plot command.



For example, if you type "set plot set polar\;" at the Mathomatic main prompt, 2D polar plots will be performed with subsequent plot commands, using variable "t" instead of "x".

Product command

Syntax: **product variable start end [step-size]**

This command performs a mathematical product (\prod) of the current expression or the RHS of the current equation as the index **variable** goes from **start** to **end** in steps of **step-size** (default 1). The result is stored and displayed. The current equation is not changed.

```
1-> y=a*x

#1: y = a*x

1-> product
Enter variable: x
x = 1
To: 10

#2: y = 3628800*(a^10)

1-> 10!
Answer = 3628800
1->
```

To see all of the intermediate results, type "set debug 1" before this.

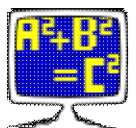
Push command

Syntax: **push [equation-number-ranges or text-to-push]**

This command pushes the current or specified equation spaces into the readline history, for easy editing and re-entry by using the cursor keys. The equation spaces are not modified. After this command, the pushed expressions are accessed by pressing the cursor UP (up arrow) key.

If any one of the arguments is not a valid equation number range, the text string containing all arguments is pushed into the readline history.

This command only exists if Mathomatic was compiled with readline support.



Quit command

Syntax: **quit** [**exit-value**]

Alternate command name: **exit**

Type in this command to exit Mathomatic. All expressions in memory are discarded. To save all your expressions stored in equation spaces, use the save command before quitting.

The optional decimal **exit value** argument is the exit status returned to the operating system. The default is 0, meaning OK.

Another way to quickly exit Mathomatic is to enter your operating system's End-Of-File (EOF) character at the beginning of an input line. The EOF character for Unix-like operating systems is Control-D.

Read command

Syntax: **read** **file-name**

This command reads in a text file as if you typed the text of the file in at the main prompt. The text file (also known as a script) should contain Mathomatic expressions and commands. Read commands may be nested; that is, the file read in may contain further read commands. If any command or operation returns with an error, all current read operations are aborted; this can be prevented by starting the line that returns with error with a colon (:) character.

If any command in the text file prompts for input, it will not read the input from the text file, instead it will prompt the user for the input.

Expressions saved with the save command are restored using this read command.

This command is automatically executed when you start up Mathomatic with file names on the shell command line.

The default file name extension (suffix) for Mathomatic input files is ".in". A file name extension is not required.

This command may be preceded with "repeat", which repeatedly reads a script until it fails or is aborted.



Real command

Syntax: **real** [variable]

This command copies the real part of a complex number expression to the next available equation space. If the current expression or RHS of the current equation is not complex, the warning message "Expression is not a mix" will be displayed. A complex number expression contains both imaginary and real number parts. To copy only the imaginary number part, see the imaginary command.

The separation **variable** may be specified on the command line, the default is the imaginary unit **i**.

There will be no imaginary numbers in the result.

```
1-> (a+b*i)/(c+d*i)
```

```
      (a + (b*i))
#1:  -----
      (c + (d*i))
```

```
1-> real
```

```
      ((a*c) + (b*d))
#2:  -----
      (c^2 + d^2)
```

```
2->
```

Repeat command

Syntax: **repeat command arguments**

Any command may be preceded by "repeat", which sets the repeat flag for that command. Many commands ignore the repeat flag, if repeating them doesn't make sense. Sometimes repeating means do a full simplify when simplifying, for example in the simplify, compare, and "solve verify" commands, etc.

Currently the calculate, compare, divide, echo, eliminate, fraction, read, roots, simplify, and solve commands do not ignore the repeat flag.



Replace command

Syntax: **replace** [**variables** ["with" **expression**]]

By default, this command prompts you for a replacement expression for each variable in the current expression or equation. If an empty line is entered for a variable, that variable remains unchanged. The result is placed in the current expression or equation and displayed.

This command is very useful for renaming or substituting variables. It is smart enough to do variable interchange.

If **variables** are specified on the command line, you will be prompted for those variables only and all other variables will be left unchanged.

If "with" is specified, you won't be prompted and all **variables** specified will be replaced with the **expression** that follows.

Roots command

Syntax: **roots** **root** **real-part** **imaginary-part**

This command displays all complex number roots of a given positive integer **root** of a complex number. The number of the **root** equals the number of correct solutions. For example, "3" would give the 3 roots of the cube root. This command will also convert rectangular coordinates to polar coordinates.

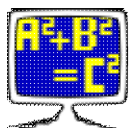
The floating point **real part** (X coordinate) and **imaginary part** (Y coordinate) of the complex number are prompted for. Just enter an empty line if the value is zero. The polar coordinates of the given complex number are displayed first, which consist of an amplitude (distance from the origin) and an angle (direction). Then each root is calculated and displayed, along with an "Inverse check" value, which should equal the original complex number. The "Inverse check" is calculated by repeated complex number multiplication of the root times itself.

Since double precision floating point is used, the results are only accurate from 10 to 12 decimal digits.

```
1-> roots
Enter root (positive integer): 3
Enter real part (X): 8
Enter imaginary part (Y):
```

```
The polar coordinates before root taking are:
8 amplitude and 0 radians (0 degrees).
```

```
The 3 roots of (8)^(1/3) are:
```



```

2
Inverse check: 8

-1 +1.73205080757*i
Inverse check: 8

-1 -1.73205080757*i
Inverse check: 8

1->

```

Save command

Syntax: **save** **file-name**

This command saves all expressions in all equation spaces into the specified text file. If the file exists, Mathomatic will ask you if you want to overwrite it. The saved expressions and equations can be reloaded (restored) at a later time by using the read command. You can edit the saved expressions with your favorite ASCII text editor.

Another way to save all equation spaces exactly as they are is to enter:

```
list hex all >file-name
```

into the main Mathomatic prompt, however this saves all constants in hexadecimal and it always overwrites "file-name". Because internally constants are binary, hexadecimal can represent them exactly. Reading in the result of this command should result in exactly the same expressions in the same equation spaces.

Set command

Syntax: **set** [{"no"}] **option** [**value**] ...

This command sets various options listed below, for the current session. They remain in effect until you exit Mathomatic. Typing "set" without arguments shows all current option settings.

The specified **option** is turned on, unless it is preceded by "no", which turns it off. Some options can be followed by a number and some options can be followed by text, setting that option to the following **value**.

To permanently change the default settings of Mathomatic, set options can be put in the file `~/.mathomaticrc` (for Microsoft Windows: `mathomatic.rc` in the same directory as the Mathomatic executable or in the \$HOME



directory). It should be a text file with one set option per line, without the word "set". That file is loaded every time Mathomatic starts up, when not in test mode. The command "set **save**" conveniently saves all current session options in that file, making them permanent. "set no **save**" removes that file, so then Mathomatic will start up with all options set to the defaults.

Options:

"set **precision**" followed by an integer less than or equal to 15 sets the display precision in number of decimal digits for most numerical output. All arithmetic in Mathomatic is double precision floating point, so it is not useful to set this higher than 15 digits. Display output is rounded to the precision set by this option, though internally all constants are rounded to fit in a double precision float data type of about 15 decimal digits precision. The default for this display "precision" set variable is 14 digits.

"set no **autosolve**" will turn off solving by typing the solve variable at the main prompt, unless an equals sign (=) is included. This allows entry of single variable expressions into equation spaces. Solving is always allowed using the solve command.

"set no **autocalc**" will turn off automatic approximation and display with the calculate command of purely numerical input entered at the main prompt. Numerical expressions are not automatically cleared from memory when this option is turned off.

"set no **autoselect**" will turn off selecting of equation spaces by just typing in the equation number. Selecting is still possible using the # operator.

"set **auto**" and "set no **auto**" turn on and off all three of the above options at once. If turned off, all expressions entered at the main prompt will be entered into equation spaces, so they can be operated on by Mathomatic commands.

"set **debug**" followed by an integer sets the debug level number. The initial debug level is 0, for no debugging. If the level number is 2 ("set debug=2"), Mathomatic will show you how it solves equations. Level 4 debugs the simplify command and its polynomial routines. Levels 5 and 6 show all intermediate expressions. Set the debug level to -1 for suppression of warnings and helpful messages.

"set **case_sensitive**" will set alphabetic case sensitive mode, while "set no case" will set case insensitive mode (all alphabetic characters will be converted to lower case). "set case" is the default.

"set **color**" enables color mode. When color mode is on, ANSI color escape sequences are output to make expressions easier to read. Requires a terminal emulator that supports ANSI color escape sequences. Put the line "no color" in your `~/.mathomaticrc` file to always startup Mathomatic with color mode disabled, unless the **-c** or **-b** option is given.



"set **bold_colors**" enables highlighting in color mode. It makes all output brighter. Use this if any colors are difficult to see. This command can be shortened to "set bold". The **-b** option also sets this.

"set **columns**" followed by a positive integer sets the expected number of character columns (width) on a terminal screen with line wrap. When an expression is to be displayed in multi-line fraction format (two-dimensional) and it is wider than this number of screen columns, single-line format is used instead, because otherwise the expression would not display properly due to wrap-around. "set no columns" or "set columns=0" does no checking for screen size and always displays in fraction format, which is useful for a terminal that doesn't wrap lines. In most cases, this value is set automatically to be the correct width on startup, or by typing "set columns". This value only affects 2D expression output.

"set **wide**" sets the number of screen columns (like "set columns=0" above does) and screen rows to 0, so that no checking for screen size is done, forcing 2D display of expressions that are too wide to display properly on a terminal with line wrap. Setting this option is useful if output is going to a file.

"set no **display2d**" will set the expression display mode to single-line format (one-dimensional) using the list command, instead of the default fraction format (two-dimensional) using the display command. Single-line format is useful when feeding Mathomatic output into another program.

fractions_display_mode is a new set option that allows controlling whether or not to display numerical fractions. It also can set the preference of simple or mixed fractions. The Mathomatic default is to display simple fractions. "set no **fractions_display**" sets the mode to 0, disabling the automatic conversion of non-integer constants like .5 to $\frac{1}{2}$ for display. "set **fractions=1**" means display some constants like .5 and 2.25 as their simple fraction equivalents: $\frac{1}{2}$ and $\frac{9}{4}$. "set **fractions=2**" means display some constants as mixed or simple fractions, for example, $\frac{9}{4}$ is displayed as $(2+\frac{1}{4})$, which is a mixed fraction.

"set no **prompt**" turns off Mathomatic prompt output, exactly like the **-q** (quiet mode) option does.

"set **preserve**" will set "preserve_surds" mode, which suppresses approximation of real roots of real rational numbers, if the result will be irrational. A surd is a quantity which can not be expressed by rational numbers. For example, $2^{\frac{1}{2}}$ (the square root of two, which is irrational and a surd) will remain $2^{\frac{1}{2}}$ unless explicitly approximated or "set no preserve" is entered. This option is turned on by default ("set preserve_surds"), allowing exact arithmetic and simplification of surds. Surds can always be manually approximated with the approximate and calculate commands.

"set **rationalize**" will set the "rationalize_denominators" option, which attempts to move radicals from the denominator of fractions to the numerator during simplification. This is the default.



"set **modulus_mode**" requires an integer from 0 to 2. When a modulus operation (%) is done on two constants: **dividend % divisor**, mode 0 returns a result that is the same sign as the dividend (same as C's % operator gives), mode 1 returns a result the same sign as the divisor (same as Python's % operator gives), mode 2 returns an always positive or zero result. Mode 2 is the default and is 100% mathematically correct and the type of modulus operation that can be generally simplified. Mode 0 is the remainder modulus used by the C and Java computer languages. This mode only affects modulus operator (%) numeric calculations. All modulus simplification rules are enabled, regardless of this mode. Modulus simplification for integer modulus expressions is always accomplished by using integer variables (variable names that start with "integer"). Not as much simplification can be done if all variables in a modulus expression are normal, non-integer variables. Modulus simplification is done by the simplify command.

"set **finance**" sets finance mode (fixed point display), which displays all constants with 2 digits after the decimal point (for example: "2.00") and negative numbers are always parenthesized (for example: "(-2.00)"). Displayed constants are rounded to the nearest cent, though internally there is no loss of accuracy until more than 15 digits have been used. The number of digits to display after the decimal point may be specified with "set finance=number". This is not truly fixed point arithmetic, it is floating point displayed as fixed point. With double precision floating point, only the most significant 15 decimal digits will ever be correct. The default is no fixed point display (finance=0).

"set **factor_integers**" sets automatic factoring of integers for all displayed expressions. When set, all integers of up to 15 decimal digits are factorized into their prime factors before the result of any command is displayed. This command can be shortened to "set factor".

"set **right_associative_power**" associates power operators from right to left in the absence of parentheses, so that x^a^b is interpreted as $x^{(a^b)}$. Other math programs typically associate power operators from right to left. The default is "set no right", which associates power operators the same as all other operators in Mathomatic, from left to right, resulting in $(x^a)^b$.

"set **plot_prefix**" followed by a string of 8-bit characters will prepend the string to the gnuplot plot string, when using the Mathomatic plot command. For example, "set plot set polar\;" typed at the Mathomatic main prompt will allow 2D polar plots with subsequent plot commands, using variable "t" instead of "x".

"set **special_variable_characters**" followed by a string of 8-bit characters will allow Mathomatic to use those characters in variable names, in addition to the normal variable name characters, which are the alphanumeric characters and underline (_). For example, "set special \$" will allow variable names like "\$a" and "a\$", and "set special []" will allow entry of array elements like "a[3]" for simulated array arithmetic. All non-alphanumeric characters in variable names are converted to underline characters (_) when exporting to a programming language or to a different program.



"set **directory**" followed by a directory name will change the current working directory to that directory. Not specifying a directory name defaults to your home directory. This command can be shortened to "set dir".

Simplify command

Syntax: **simplify** ["sign"] ["symbolic"] ["quick[est]"] ["fraction"] [equation-number-ranges]

This command fully simplifies expressions in selected equation spaces. The result is usually the smallest possible, easily readable expression that is mathematically equivalent to the original expression.

Use this command whenever you think an expression is not completely simplified or if you don't like the way an expression is factored. Sometimes simplifying more than once or using the "symbolic" option simplifies even more. This command always tries to factor polynomials, if it will make the expression smaller, unless the "**quickest**" option is given.

More than one option may be specified at a time.

Options:

"simplify **sign**" conveniently expands all "sign" variables by substituting them with all possible combinations of values (+1 and -1), storing the unique results into new equation spaces and fully simplifying. This will effectively create one simplified equation for each solution.

The "**symbolic**" option indicates $(a^n)^m$ should always be reduced to $a^{(n*m)}$. This often simplifies more and removes any absolute value operations: $((a^2)^.5 = a^{(2*.5)} = a^1 = a)$. Try this "symbolic" option if the simplify command doesn't simplify well, it often helps with powers raised to powers, though it is sometimes not 100% mathematically correct.

The "**quick**" option skips expanding sums raised to the power of 2 or higher, like $(x+1)^5$. Also, algebraic fractions might be simpler with this option, unlike denominators are not combined. This option often simplifies the best.

The "**quickest**" option very basically simplifies without any unfactoring nor factoring. Running the simplify command with this option makes it complete almost instantaneously.

"simplify **fraction**" fully simplifies any expression with division in it down to the ratio of two polynomials or expressions, like Maxima's ratsimp() function does. The result will be a single simple algebraic fraction, like the fraction command produces, the difference here being it



will be completely simplified. This is accomplished by full simplification without doing "unfactor fraction" and without doing polynomial or smart (algebraic) division on the divide operators.

This simplify command applies many algebraic transformations and their inverses (for example, unfactor and then factor) and then tries to combine and reduce algebraic fractions and rationalize their denominators. Complex fractions are converted to simple fractions by making the denominators of fractions added together the same, combining and simplifying. Polynomials with repeated or symbolic factors are factored next. Then smart (heuristic) division and polynomial division are tried on any algebraic divides, possibly making complex fractions if it reduces the expression size. Lastly, the expressions are nicely factored and displayed.

Smart division is a symbolic division like polynomial division, but it tries every term in the dividend, instead of only the term with the base variable raised to the highest power, to make the expression smaller.

"repeat simplify" repeatedly runs the simplify command until the result stabilizes to the smallest size expression. In other computer algebra systems, this is called full simplification.

Solve command

Syntax: `solve ["verify"] [equation-number-range] ["for"] variable or "0"`

This command automatically solves the specified equations for the specified **variable** or for zero. For each successful solve operation, the equation solved is replaced with the solution, becomes the current equation and is displayed. See the section on Solving Equations for more information on solving with Mathomatic.

Solving for **variable**² or **0**² will isolate the square root of the largest expression containing the specified variable, and then square both sides of the equation. This is a new feature for properly squaring, cubing, etc. both sides of an equation, and it works for any power and variable with any equation with roots.

The "**verify**" option checks the result of solving for a variable by plugging all solutions into the original equation and then simplifying and comparing. If the resulting equation sides are identical (an identity), a "Solutions verified" message is displayed, meaning that all of the solutions are correct. Otherwise "Solution may be incorrect" is displayed, meaning at least one of the solutions is incorrect or unverifiable. The "verify" option only works when solving for a single variable, and indicates if the solve result can be trusted.

The "**for**" option has no additional effect and is to make entering this solve command more natural.

Sum command

Syntax: `sum variable start end [step-size]`

Options:



This command performs a mathematical summation (Σ) of the current expression or the RHS of the current equation as the index **variable** goes from **start** to **end** in steps of **step-size** (default 1). The result is stored and displayed. The current equation is not changed.

```
1-> y=a*x

#1: y = a*x

1-> sum
Enter variable: x
x = 1
To: 10

#2: y = 55*a

1->
```

To see all of the intermediate results, type "set debug 1" before this.

Tally command

Syntax: **tally** ["average"]

This command prompts for a value, adds it to a running (grand) total, simplifies and displays the running total and optional average, and repeats. The average is the arithmetic mean, that is the running total divided by the number of entries. When finished, the ending total is returned in the next available equation space, displayed, and made the current equation.

It is a convenient way of adding, subtracting, and averaging many numbers and/or variables. Enter a minus sign (−) before each value you wish to subtract. Enter an empty line to end.

Taylor command

Syntax: **taylor** ["nosimplify"] **variable order point**

This command computes the Taylor series expansion of the current expression or RHS of the current equation, with respect to the specified **variable**. The Taylor series uses differentiation and is often used to approximate expressions near the specified **point**.

The Taylor series of **f(x)** at **point a** is the power series:

$$f'(a) (x - a) + \frac{f''(a)}{2!} (x - a)^2 + \frac{f'''(a)}{3!} (x - a)^3 + \dots$$



$$f(a) + \frac{\dots}{1!} + \frac{\dots}{2!} + \frac{\dots}{3!} + \dots$$

where $f'(x)$ is the first derivative of $f(x)$ with respect to x , $f''(x)$ is the second derivative, etc.

This command prompts you for the **point** of expansion, which is usually a variable or 0, but may be any expression. Typically 0 is used to generate Maclaurin polynomials.

Then it prompts you for the **order** of the series, which is an integer indicating how many derivatives to take in the expansion. The default is a large number, stopping when the derivative reaches 0.

The result is simplified unless the "nosimplify" option is specified, and placed in the next available equation space, displayed, and becomes the current equation. The original expression is not modified.

```
1-> e^x
```

```
#1: e^x
```

```
1-> taylor x
```

```
Taylor series expansion around x = point.
```

```
Enter point: 0
```

```
Enter order (number of derivatives to take): 8
```

```
Computing the Taylor series and simplifying...
```

```
8 derivatives applied.
```

```
#2: 1 + x +  $\frac{x^2}{2}$  +  $\frac{x^3}{6}$  +  $\frac{x^4}{24}$  +  $\frac{x^5}{120}$  +  $\frac{x^6}{720}$  +  $\frac{x^7}{5040}$  +  $\frac{x^8}{40320}$ 
```

```
2->
```

Unfactor command

Syntax: **unfactor** ["count"] ["fraction"] ["quick"] ["power"] [equation-number-range]

Alternate command name: **expand**

This command algebraically expands expressions in selected equation spaces by multiplying out products of sums and exponentiated sums and then simplifying a little, displaying the results. One or more options may be specified, like "count", which also displays the number of additive terms.

To illustrate what unfactoring does, suppose you have the following equations:

```
1-> a=b*(c+d)
```

```
#1: a = b*(c + d)
```



```

1-> z=(x+y)^2

#2: z = (x + y)^2

2-> unfactor all

#1: a = (b*c) + (b*d)

#2: z = (x^2) + (2*x*y) + (y^2)

2->

```

$(x+y)^2$ is called an exponentiated sum and is converted to $(x+y)*(x+y)$ and then multiplied out, unless the "**quick**" option is given. Because this is a general but inefficient expansion method, exponentiated sums usually fail expansion when the power is greater than 10, growing larger than will fit in an equation space. "unfactor **quick**" only expands products of sums, and not exponentiated sums.

The opposite of unfactoring is factoring. Careful and neat factoring is always done by the simplify command.

"unfactor **fraction**" by itself expands algebraic fractions by also expanding division of sums, multiplying out each fraction with a sum in the numerator into the sum of smaller fractions with the same denominator for each term in numerator. See the example under the fraction command.

"unfactor **power**" does only power operator expansion; that is, $(a*b)^{(n+m)}$ is transformed to $(a^n)*(a^m)*(b^n)*(b^m)$.

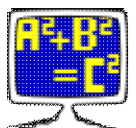
Variables command

Syntax: **variables** ["c" or "java" or "integer" or "count"] [equation-number-ranges]

Show or define all variable names used within the specified expressions, from most frequent to least frequently occurring. The programming language options output the variable definitions required to make code from the specified equations. This does not initialize any variables, it only defines them as needed for a C or Java compiler. This command is not necessary for generating Python code.

The "count" option displays the total counts of each variable in the specified expressions. The count means the number of times the variable occurs.

With no options, or the "count" option, this command returns false (with an error message) if no normal variables were found. This may be useful for determining whether an expression is numeric or symbolic.



Version command

Syntax: **version**

Shows the version number, compilation options used, expression array size, maximum possible memory usage, invoked security level, and license summary, for the currently running version of Mathomatic. The maximum memory usage displayed is the amount of RAM used when all equation spaces have been filled. It does not include stack size (which varies) or executable (code) size.

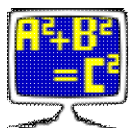
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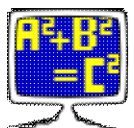
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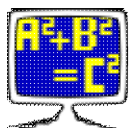
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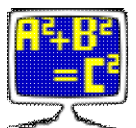
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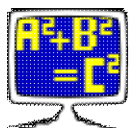


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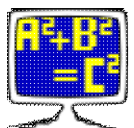
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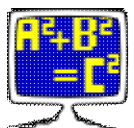
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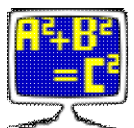
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